



# Recommender Systems & Embeddings

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# Outline

**Embeddings**

**Dropout Regularization**

**Recommender Systems**

# Embeddings

# Symbolic variable

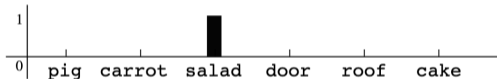
- Text: characters, words, bigrams...
- Recommender Systems: item ids, user ids
- Any categorical descriptor: tags, movie genres, visited URLs, skills on a resume, product categories...

## Notation:

Symbol  $s$  in vocabulary  $V$

# One-hot representation

$$\text{onehot}(\text{'salad'}) = [0, 0, 1, \dots, 0] \in \{0, 1\}^{|V|}$$



- Sparse, discrete, large dimension  $|V|$
- Each axis has a meaning
- Symbols are equidistant from each other:

$$\text{euclidean distance} = \sqrt{2}$$

# Embedding

$$\text{embedding}(\text{'salad'}) = [3.28, -0.45, \dots 7.11] \in \mathbb{R}^d$$

- Continuous and dense.
- Can represent a huge vocabulary in low dimension, typically:  
 $d \in \{16, 32, \dots, 4096\}$ .
- Axis have no meaning *a priori*.
- Embedding metric can capture semantic distance.

**Neural Networks compute transformations on continuous vectors**

# Implementation with Keras

Size of vocabulary  $n = |V|$ , size of embedding  $d$

```
# input: batch of integers
```

```
Embedding(output_dim=d, input_dim=n, input_length=1)
```

```
# output: batch of float vectors
```

- Equivalent to one-hot encoding multiplied by a weight matrix

$$\mathbf{W} \in \mathbb{R}^{n \times d}:$$

$$\text{embedding}(x) = \text{onehot}(x) \cdot \mathbf{W}$$

- $\mathbf{W}$  is typically **randomly initialized**, then **tuned by backprop**
- $\mathbf{W}$  are trainable parameters of the model

# Distance and similarity in Embedding space

## Euclidean distance

$$d(x, y) = ||x - y||_2$$

- Simple with good properties
- Dependent on norm (embeddings usually unconstrained)

## Cosine similarity

$$\text{cosine}(x, y) = \frac{x \cdot y}{||x|| \cdot ||y||}$$

- Angle between points, regardless of norm
- $\text{cosine}(x, y) \in (-1, 1)$
- Expected cosine similarity of random pairs of vectors is 0

# Distance and similarity in Embedding space

If  $x$  and  $y$  both have unit norms:

$$||x - y||_2^2 = 2 \cdot (1 - \text{cosine}(x, y))$$

or alternatively:

$$\text{cosine}(x, y) = 1 - \frac{||x - y||_2^2}{2}$$

Alternatively, dot product (unnormalized) is used in practice as a pseudo similarity

# Visualizing Embeddings

- Visualizing requires a projection in 2 or 3 dimensions
- Objective: visualize which embedded symbols are similar

## PCA

- Limited by linear projection, embeddings usually have complex high dimensional structure

## t-SNE

Visualizing data using t-SNE, L van der Maaten, G Hinton, *The Journal of Machine Learning Research*, 2008

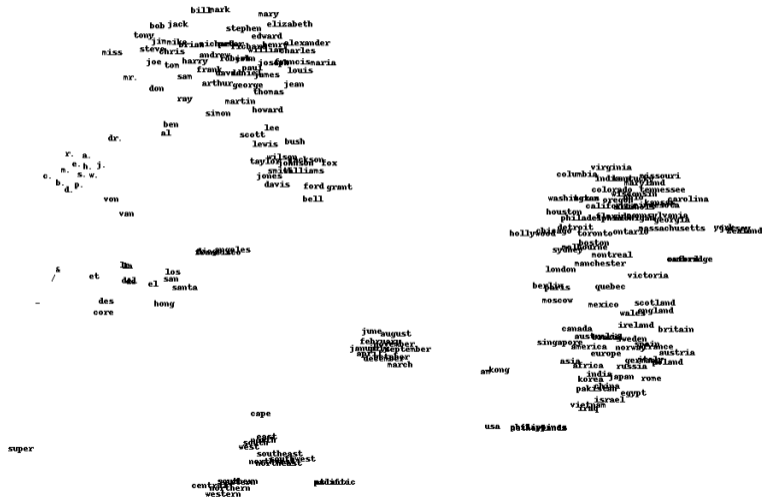
# t-Distributed Stochastic Neighbor Embedding

- Unsupervised, low-dimension, non-linear projection
- Optimized to preserve relative distances between nearest neighbors
- Global layout is not necessarily meaningful

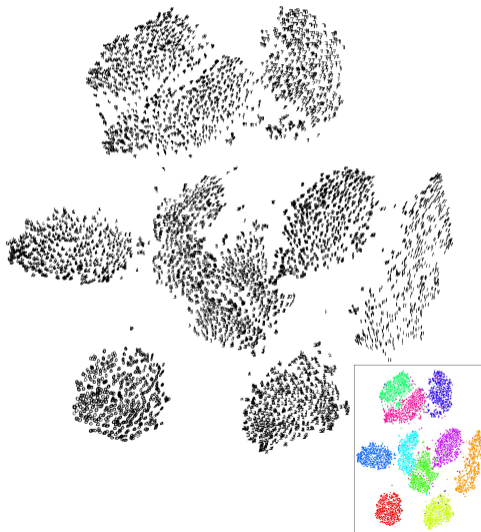
## **t-SNE projection is non deterministic (depends on initialization)**

- Critical parameter: perplexity, usually set to 20, 30
- See <http://distill.pub/2016/misread-tsne/>

# Example word vectors



# Visualizing Mnist



# Dropout Regularization

# Regularization

**Size of the embeddings**

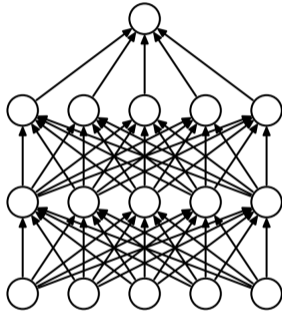
**Depth of the network**

**$L_2$  penalty on embeddings**

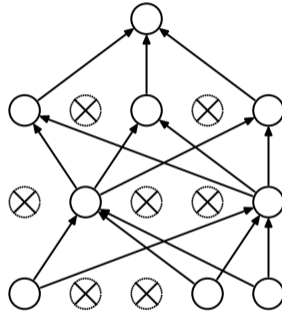
**Dropout**

- Randomly set activations to 0 with probability  $p$
- Bernoulli mask sampled for a forward pass / backward pass pair
- Typically only enabled at training time

# Dropout



(a) Standard Neural Net



(b) After applying dropout.

Dropout: A Simple Way to Prevent Neural Networks from Overfitting, Srivastava et al., *Journal of Machine Learning Research* 2014

# Dropout

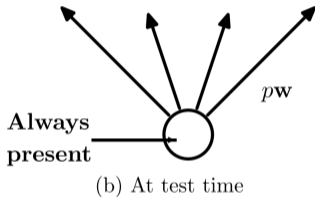
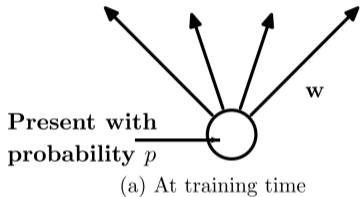
## Interpretation

- Reduces the network dependency to individual neurons
- More redundant representation of data

## Ensemble interpretation

- Equivalent to training a large ensemble of shared-parameters, binary-masked models
- Each model is only trained on a single data point

# Dropout

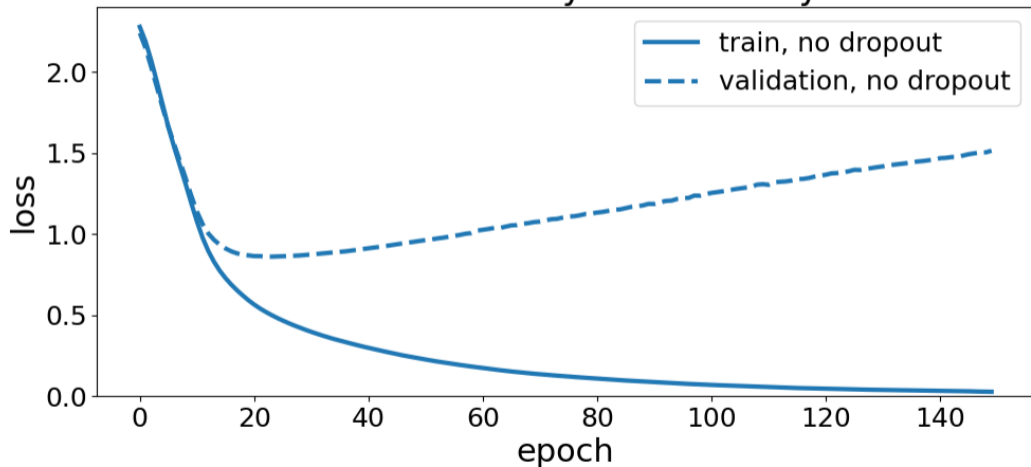


At test time, multiply weights by  $p$  to keep same level of activation.

Dropout: A Simple Way to Prevent Neural Networks from Overfitting, Srivastava et al., *Journal of Machine Learning Research* 2014

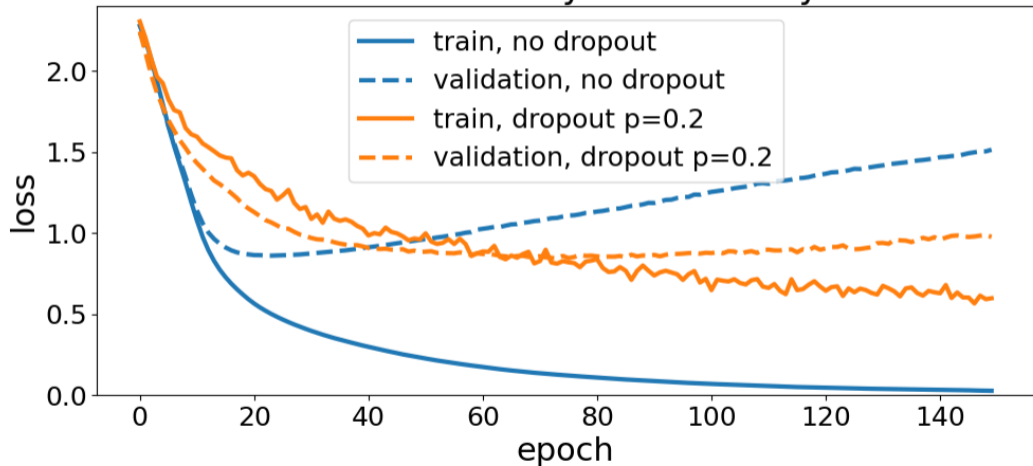
# Overfitting Noise

MLP with 3 hidden layers and noisy labels



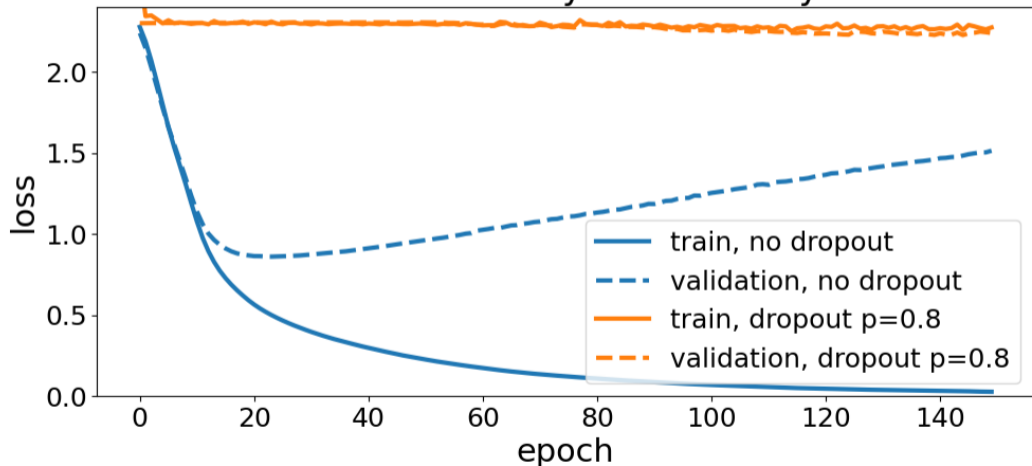
# A bit of Dropout

MLP with 3 hidden layers and noisy labels



# Too much: Underfitting

MLP with 3 hidden layers and noisy labels



# Implementation with Keras

```
model = Sequential()  
model.add(Dense(hidden_size, input_shape, activation='relu'))  
model.add(Dropout(p=0.5)) # <=====  
model.add(Dense(hidden_size, activation='relu'))  
model.add(Dropout(p=0.5)) # <=====  
model.add(Dense(output_size, activation='softmax'))
```

# Recommender Systems

# Recommender Systems

## **Recommend contents and products**

Movies on Netflix and YouTube, weekly playlist and related Artists on Spotify, books on Amazon, related apps on app stores, “Who to Follow” on twitter...

## **Prioritized social media status updates**

## **Personalized search engine results**

## **Personalized ads and RTB**

# RecSys

## Content-based vs Collaborative Filtering (CF)

**Content-based:** user metadata (gender, age, location...) and item metadata (year, genre, director, actors)

**Collaborative Filtering:** passed user/item interactions: stars, plays, likes, clicks

**Hybrid systems:** CF + metadata to mitigate the cold-start problem

# Explicit vs Implicit Feedback

**Explicit:** positive and negative feedback

- Examples: review stars and votes
- Regression metrics: Root Mean Squared Error (RMSE), Mean Absolute Error (MAE)...

**Implicit:** positive feedback only

- Examples: page views, plays, comments...
- Ranking metrics: ROC AUC, precision at rank, NDCG...

# Explicit vs Implicit Feedback

**Implicit** feedback much more **abundant** than explicit feedback

Explicit feedback does not always reflect **actual user behaviors**

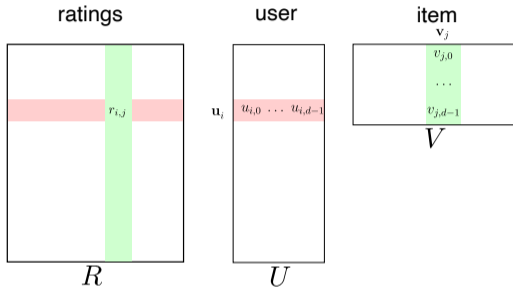
- Self-declared independent movie enthusiast but watch a majority of blockbusters

**Implicit** feedback can be **negative**

- Page view with very short dwell time
- Click on “next” button

Implicit (and Explicit) feedback distribution **impacted by UI/UX changes** and the **RecSys deployment** itself.

# Matrix Factorization for CF

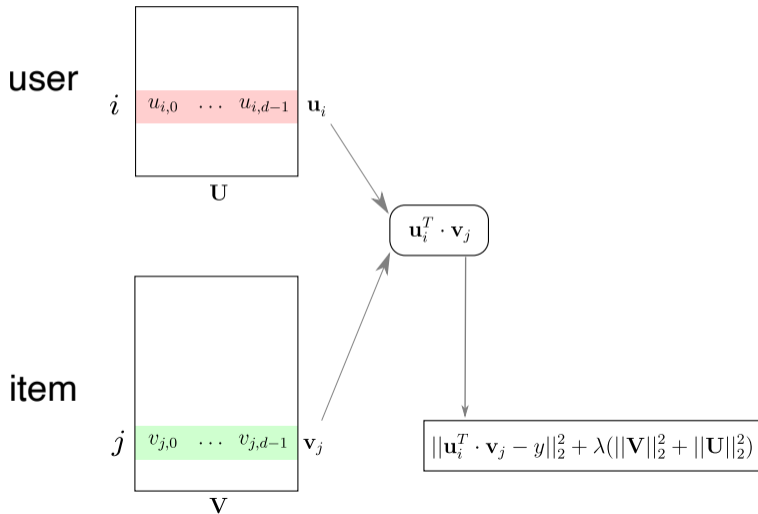


$$L(U, V) = \sum_{(i,j) \in D} \|\mathbf{r}_{i,j} - \mathbf{u}_i^\top \cdot \mathbf{v}_j\|_2^2 + \lambda(\|U\|_2^2 + \|V\|_2^2)$$

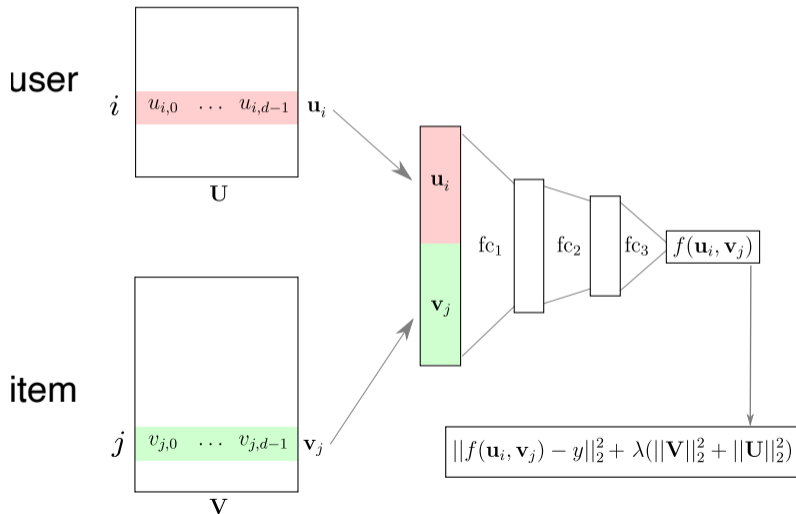
- Train  $U$  and  $V$  on observed ratings data  $r_{i,j}$
- Use  $U^\top V$  to find missing entries in sparse rating data matrix  $R$

# **Architecture and Regularization**

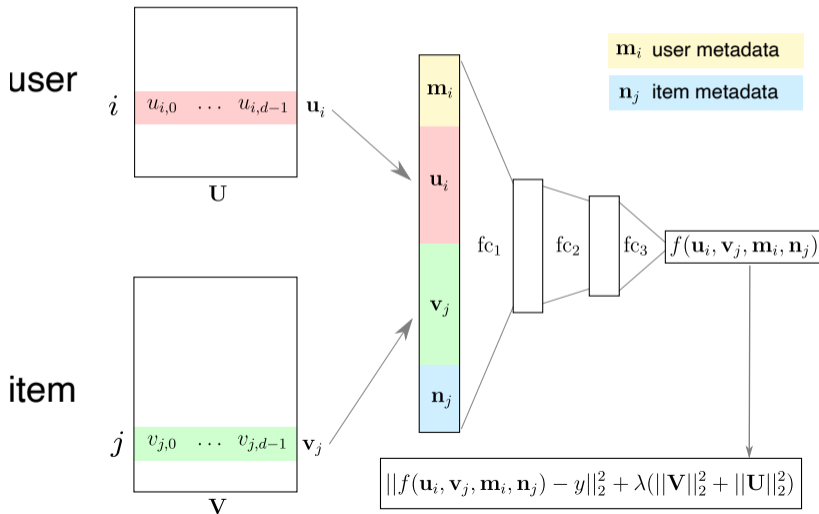
# RecSys with Explicit Feedback



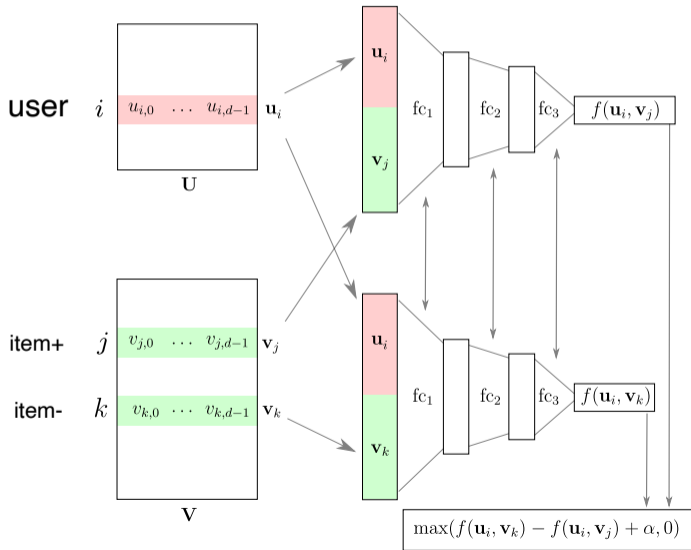
# Deep RecSys Architecture



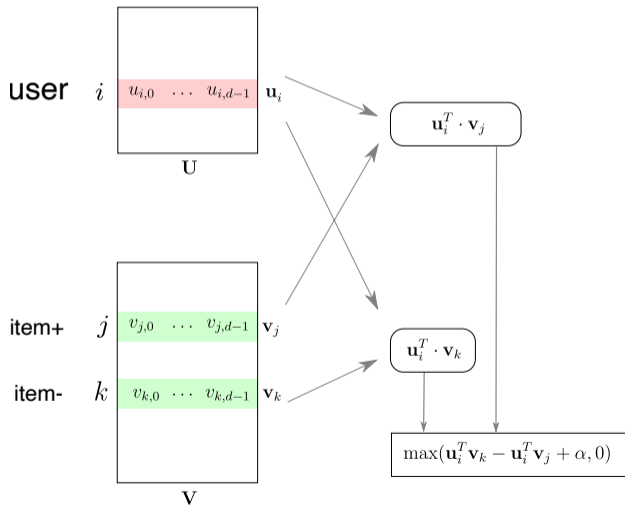
# Deep RecSys with metadata



# Implicit Feedback: Triplet loss

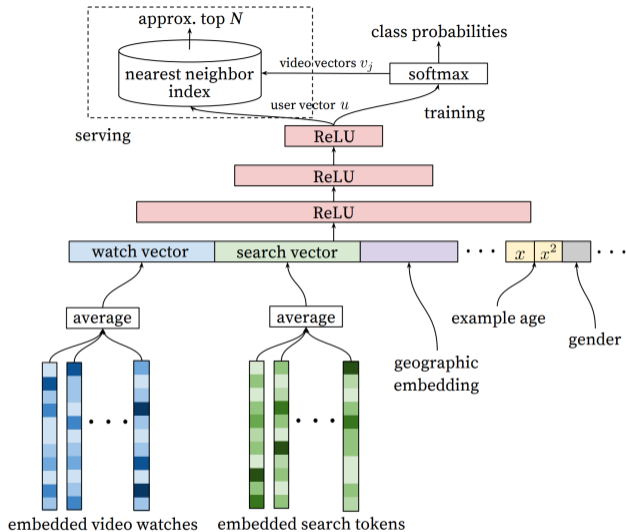


# Deep Triplet Networks



# Training a Triplet Model

- Gather a set of positive pairs user  $i$  and item  $j$
- While model has not converged:
  - Shuffle the set of pairs  $(i, j)$
  - For each  $(i, j)$ :
    - ▶ Sample item  $k$  uniformly at random
    - ▶ Call item  $k$  a negative item for user  $i$
    - ▶ Train model on triplet  $(i, j, k)$



Deep Neural Networks for YouTube Recommendations

<https://research.google.com/pubs/pub45530.html>

# **Ethical Considerations of Recommender Systems**

# Ethical Considerations

## Amplification of existing discriminatory and unfair behaviors / bias

- Example: gender bias in ad clicks (fashion / jobs)
- Using the firstname as a predictive feature

## Amplification of the filter bubble and opinion polarization

- Personalization can amplify “people only follow people they agree with”
- Optimizing for “engagement” promotes content that causes strong emotional reaction (and turns normal users into *haters*?)
- RecSys can exploit weaknesses of some users, lead to addiction
- Addicted users clicks over-represented in future training data

# Call to action

## Designing Ethical Recommender Systems

- Wise modeling choices (e.g. use of “firstname” as feature)
- Conduct internal audits to detect fairness issues: SHAP, Integrated Gradients, fairlearn.org
- Learning representations that enforce fairness?

## Transparency

- Educate decision makers and the general public
- How to allow users to assess fairness by themselves?
- How to allow for independent audits while respecting the privacy of users?